

$$D_x(u + v) = D_x u + D_x v$$

$$\frac{d}{dx}(x^3 + x^4) = 3x^2 + 4x^3$$

$$D_x u^n = nu^{n-1} D_x u$$

$$\frac{d}{dx} x^3 = 3x^2$$

Product Rule

$$D_x(uv) = uD_x v + vD_x u$$

$$\frac{d}{dx}(x^3 \cdot x^4) = x^3(4x^3) + x^4(3x^2)$$

Quotient Rule

$$D_x \left(\frac{u}{v} \right) = \frac{vD_x u - uD_x v}{v^2}$$

$$\frac{d}{dx} \left(\frac{x^3}{x^4} \right) = \frac{x^4(3x^2) - x^3(4x^3)}{(x^4)^2}$$

$$D_x \sin u = \cos u D_x u$$

$$\frac{d}{dx} \sin x = \cos x$$
$$\frac{d}{dx} \sin x^2 = (\cos x^2)(2x)$$

$$D_x \cos u = -\sin u D_x u$$

$$\frac{d}{dx} \cos x = -\sin x$$
$$\frac{d}{dx} \cos x^2 = (-\sin x^2)(2x)$$

$$D_x \tan u = \sec^2 u D_x u$$

$$\frac{d}{dx} \tan x = \sec^2 x$$
$$\frac{d}{dx} \tan x^2 = [\sec^2(x^2)](2x)$$

$$D_x \cot u = -\csc^2 u D_x u$$

$$\frac{d}{dx} \cot x = -\csc^2 x$$
$$\frac{d}{dx} \cot x^2 = [-\csc^2 x^2](2x)$$

$$D_x \sec u = \sec u \tan u D_x u$$

$$\frac{d}{dx} \sec x \tan x$$
$$\frac{d}{dx} \sec x^2 = (\sec x^2 \tan x^2) (2x)$$

$$D_x \csc u = -\csc u \cot u D_x u$$

$$\frac{d}{dx} \csc x = -\csc x \cot x$$
$$\frac{d}{dx} \csc x^2 = (-\csc x^2 \cot x^2)(2x)$$

$$D_x \sinh u = \cosh u D_x u$$

$$\frac{d}{dx} \sinh x = \cosh x$$
$$\frac{d}{dx} \sinh x^2 = (\cosh x^2)(2x)$$

$$\sinh x = \frac{e^x - e^{-x}}{2}$$

$$\cosh x = \frac{e^x + e^{-x}}{2}$$

$$\tanh x = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$

$$\operatorname{csch} x = \frac{2}{e^x - e^{-x}}$$

$$\operatorname{sech} x = \frac{2}{e^x + e^{-x}}$$

$$\coth x = \frac{e^x + e^{-x}}{e^x - e^{-x}}$$

$$D_x \cosh u = \sinh u D_x u$$

$$D_x \tanh u = \operatorname{sech}^2 u D_x u$$

$$D_x \coth u = -\operatorname{csch}^2 u D_x u$$

$$\begin{aligned} \frac{d}{dx} \cosh x &= \sinh x \\ \frac{d}{dx} \cosh x^2 &= (\sinh x^2)(2x) \end{aligned}$$

$$\begin{aligned} \frac{d}{dx} \tanh x &= \operatorname{sech}^2 x \\ \frac{d}{dx} \tanh x^2 &= (\operatorname{sech}^2 x^2)(2x) \end{aligned}$$

$$\begin{aligned} \frac{d}{dx} \coth x &= -\operatorname{csch}^2 x \\ \frac{d}{dx} \coth x^2 &= (-\operatorname{csch}^2 x^2)(2x) \end{aligned}$$

$$D_x \operatorname{sech} u = -\operatorname{sech} u \tanh u D_x u$$

$$\frac{d}{dx} \operatorname{sech} x = -\operatorname{sech} x \tanh x$$
$$\frac{d}{dx} \operatorname{sech} x^2 = (-\operatorname{sech} x^2 \tanh x^2)(2x)$$

$$D_x \operatorname{csch} u = -\operatorname{csch} u \operatorname{coth} u D_x u$$

$$\frac{d}{dx} \operatorname{csch} x = -\operatorname{csch} x \operatorname{coth} x$$
$$\frac{d}{dx} \operatorname{csch} x^2 = (-\operatorname{csch} x^2 \operatorname{coth} x^2)(2x)$$

$$D_x e^u = e^u D_x u$$

$$\frac{d}{dx} e^x = e^x$$
$$\frac{d}{dx} e^{x^2} = e^{x^2} (2x)$$

$$D_x a^u = a^u \ln a D_x u$$

$$\frac{d}{dx} 3^x = 3^x \ln 3$$
$$\frac{d}{dx} 3^{x^2} = (3^{x^2} \ln 3)(2x)$$

$$D_x \log_a u = \frac{D_x u}{u \ln a}$$

$$\frac{d}{dx} \log_3 x = \frac{1}{x \ln 3}$$
$$\frac{d}{dx} \log_3 x^2 = \left(\frac{1}{x^2 \ln 3} \right) (2x)$$

Change of base formula

$$\log_b x = \frac{\log x}{\log b} = \frac{\ln x}{\ln b}$$

$$D_x \ln u = \frac{D_x u}{u}$$

$$\frac{d}{dx} \ln x = \frac{1}{x}$$
$$\frac{d}{dx} \ln x^2 = \left(\frac{1}{x^2} \right) (2x)$$

$$D_x \sin^{-1} u = \frac{D_x u}{\sqrt{1 - u^2}}$$

$$\frac{d}{dx} \sin^{-1} x = \frac{1}{\sqrt{1 - x^2}}$$

$$D_x \cos^{-1} u = \frac{-D_x u}{\sqrt{1 - u^2}}$$

$$\frac{d}{dx} \cos^{-1} x = \frac{-1}{\sqrt{1 - x^2}}$$

$$D_x \tan^{-1} u = \frac{D_x u}{1 + u^2}$$

$$\frac{d}{dx} \tan^{-1} x = \frac{1}{1 + x^2}$$

$$D_x \cot^{-1} u = \frac{-D_x u}{1 + u^2}$$

$$\frac{d}{dx} \cot^{-1} x = \frac{-1}{1 + x^2}$$

$$D_x \sec^{-1} u = \frac{D_x u}{|u| \sqrt{u^2 - 1}}$$

$$\frac{d}{dx} \sec^{-1} x = \frac{1}{|x| \sqrt{x^2 - 1}}$$

$$D_x \csc^{-1} u = \frac{-D_x u}{|u|\sqrt{u^2 - 1}}$$

$$\frac{d}{dx} \csc^{-1} x = \frac{-1}{|x|\sqrt{x^2 - 1}}$$

$$D_x \int_a^u f(t) dt = f(u) D_x u$$

$$\frac{d}{dx} \int_0^x f(t) dt = f(x)$$
$$\frac{d}{dx} \int_0^{x^2} f(t) dt = [f(x)](2x)$$

$$\cos^2 \theta + \sin^2 \theta = 1$$

$$1 + \tan^2 \theta = \sec^2 \theta$$

$$1 + \cot^2 \theta = \csc^2 \theta$$

$$\sin(-\theta) = -\sin(\theta)$$

$$\cos(-\theta) = \cos(\theta)$$

$$\tan(-\theta) = -\tan(\theta)$$

$$\cot(-\theta) = -\cot(\theta)$$

$$\sec(-\theta) = \sec(\theta)$$

$$\csc(-\theta) = -\csc(\theta)$$

$$\sin(2\theta) = 2 \sin \theta \cos \theta$$

$$\cos(2\theta) = \begin{cases} 2 \cos^2 \theta - 1 \\ 1 - 2 \sin^2 \theta \\ \cos^2 \theta - \sin^2 \theta \end{cases}$$

$$\cos^2 \theta = \frac{1}{2}(1 + \cos(2\theta))$$

$$\sin^2 \theta = \frac{1}{2}(1 - \cos(2\theta))$$

$$\sin(A + B) = \sin A \cos B + \sin B \cos A$$

$$\sin(A - B) = \sin A \cos B - \sin B \cos A$$

$$\cos(A + B) = \cos A \cos B - \sin A \sin B$$

$$\cos(A - B) = \cos A \cos B + \sin A \sin B$$

$$\tan(A + B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\tan(A - B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

$$\sin A \cos B = \frac{1}{2} [\sin(A + B) + \sin(A - B)]$$

$$\cos A \cos B = \frac{1}{2} [\cos(A + B) + \cos(A - B)]$$

$$\sin A \sin B = \frac{1}{2} [\cos(A - B) - \cos(A + B)]$$

$$\cos A \sin B = \frac{1}{2} [\sin(A + B) - \sin(A - B)]$$

$$\tan A \tan B = \frac{\cos(A - B) - \cos(A + B)}{\cos(A - B) + \cos(A + B)}$$

$$\int u^n du = \frac{u^{n+1}}{n+1} + C$$

$$\int x^3 dx = \frac{x^4}{4} + C$$

$$\int \frac{1}{u} du = \ln|u| + C$$

$$\int \frac{1}{x} dx = \ln|x| + C$$

$$\int \sin u \, du = -\cos u + C$$

$$\int \sin x \, dx = -\cos x + C$$

$$\int \cos u \, du = \sin u + C$$

$$\int \cos x \, dx = \sin x + C$$

$$\int \sec^2 u \, du = \tan u + C$$

$$\int \sec^2 x \, dx = \tan x + C$$

$$\int \csc^2 u \, du = -\cot u + C$$

$$\int \csc^2 x \, dx = -\cot x + C$$

$$\int \sec u \tan u \, du = \sec u + C$$

$$\int \sec x \tan x \, dx = \sec x + C$$

$$\int \csc u \cot u \, du = -\csc u + C$$

$$\int \csc x \cot x \, dx = -\csc x + C$$

$$\int \tan u \, du = -\ln|\cos u| + C$$

$$\int \tan x \, dx = -\ln|\cos x| + C$$

$$\int \cot u \, du = \ln|\sin u| + C$$

$$\int \cot x \, dx = \ln|\sin x| + C$$

$$\int \sec u \, du = \ln |\sec u + \tan u| + C$$

$$\int \sec x \, dx = \ln |\sec x + \tan x| + C$$

$$\int \csc u = \ln |\csc u - \cot u| + C$$

$$\int \csc x = \ln |\csc x - \cot x| + C$$

$$\int \frac{1}{\sqrt{a^2 - u^2}} \, du = \sin^{-1} \frac{u}{a} + C$$

$$\int \frac{1}{\sqrt{1 - x^2}} \, dx = \sin^{-1} x + C$$

$$\int \frac{1}{\sqrt{4 - x^2}} \, dx = \sin^{-1} \frac{x}{2} + C$$

$$\int \frac{1}{\sqrt{9 - x^2}} \, dx = \sin^{-1} \frac{x}{3} + C$$

$$\int \frac{1}{a^2 + u^2} \, du = \frac{1}{a} \tan^{-1} \frac{u}{a} + C$$

$$\int \frac{1}{1 + x^2} \, dx = \tan^{-1} x + C$$

$$\int \frac{1}{4 + x^2} \, dx = \frac{1}{2} \tan^{-1} \frac{x}{2} + C$$

$$\int \frac{1}{9 + x^2} \, dx = \frac{1}{3} \tan^{-1} \frac{x}{3} + C$$

$$\int \frac{1}{u\sqrt{u^2 - a^2}} du = \frac{1}{a} \sec^{-1} \left| \frac{u}{a} \right| + C$$

$$\int \frac{1}{x\sqrt{x^2 - 1}} dx = \sec^{-1}|x| + C$$

$$\int \frac{1}{x\sqrt{x^2 - 4}} dx = \frac{1}{2} \sec^{-1} \left| \frac{x}{2} \right| + C$$

$$\int \frac{1}{x\sqrt{x^2 - 9}} dx = \frac{1}{3} \sec^{-1} \left| \frac{x}{3} \right| + C$$

$$\int \sinh u du = \cosh u + C$$

$$\int \cosh u du = \sinh u + C$$

$$\int \operatorname{sech}^2 u du = \tanh u + C$$

$$\int \operatorname{csch}^2 u \, du = -\operatorname{coth} u + C$$

$$\int \operatorname{sech} u \tanh u \, du = -\operatorname{sech} u + C$$

$$\int \operatorname{csch} u \operatorname{coth} u \, du = -\operatorname{csch} u + C$$

Integration by Parts

$$\int u \, dv = uv - \int v \, du$$

$$\int e^u du = e^u + C$$

$$\int a^u du = \frac{a^u}{\ln a} + C$$

$$\ln AB = \ln A + \ln B$$

$$\ln \frac{A}{B} = \ln A - \ln B$$

$$\ln x^k = k \ln x$$

Trig Substitution

$$\sqrt{a^2 - u^2}$$

Use $u = a \sin \theta$

Trig Substitution

$$\sqrt{a^2 + u^2}$$

Use $u = a \tan \theta$

Trig Substitution

$$\sqrt{u^2 - a^2}$$

Use $u = a \sec \theta$

Method of Circular Disks

$$V = \pi \int_a^b [f(x)]^2 dx$$

Method of Circular Rings

$$V = \pi \int_a^b \{ [f(x)]^2 - [g(x)]^2 \} dx$$

↓ ↓ ↓
Top Bottom Width
Curve Curve

Method of Cylindrical Shells

$$V = 2\pi \int_a^b x [f(x)] dx$$

↓ ↓ ↓
Distance Length Width

Arc Length

$$S = \int_a^b \sqrt{1 + [f'(x)]^2} dx$$

Surface Area

$$S.A. = 2\pi \int_a^b r(x) \sqrt{1 + [f'(x)]^2} dx$$

↓
Radius

Inverse Function Rule

$$(f^{-1})'(x) = \frac{1}{f'[f^{-1}(x)]}$$

Power Series

$$\frac{1}{1-x} = 1 + x + x^2 + x^3 + \dots = \sum_{k=0}^{\infty} x^k$$

For $|x| < 1$

Gregory's Series

$$\tan^{-1} x = x - \frac{x^3}{3} + \frac{x^5}{5} - \frac{x^7}{7} + \dots = \sum_{k=0}^{\infty} \frac{(-1)^k x^{2k+1}}{2k+1}$$

For $|x| < 1$

$$e^x = \sum_{k=0}^{\infty} \frac{x^k}{k!} = 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \frac{x^4}{4!} + \dots$$

$$\begin{aligned} \sin x &= \sum_{k=0}^{\infty} \frac{(-1)^k x^{2k+1}}{(2k+1)!} \\ &= x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \dots \end{aligned}$$

$$\begin{aligned} \cos x &= \sum_{k=0}^{\infty} \frac{(-1)^k x^{2k}}{(2k)!} \\ &= 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \dots \end{aligned}$$

$$\begin{aligned} \ln(1+x) &= \sum_{k=0}^{\infty} \frac{(-1)^k x^{k+1}}{k+1} \\ &= x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \dots \end{aligned}$$

